

# Human–Machine Cooperative Steering Control Based on Non-cooperative Nash Game

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## Abstract

To address the conflict of inconsistent driving intentions between the driver and driving assistance system in cooperative steering, a human–machine cooperative steering control framework based on non-cooperative Nash game is proposed. The competitive relationship between the driver and driving assistance system with different control objectives is modeled as a non-cooperative Nash game. The cooperative steering under human–machine Nash game condition is transformed into a model predictive control optimization problem to achieve coordination through Nash equilibrium. A flexible driving authority allocation strategy based on time-to-collision is then proposed for vehicle lateral control, with dynamic driving authority weights fed into the human–machine cooperative steering model in real time. The effectiveness of the non-cooperative Nash game human–machine cooperative steering strategy and flexible driving authority allocation strategy is validated through simulations and hardware-in-the-loop experiments. Results show the proposed strategy can improve vehicle safety while retaining certain driver freedom when human–machine control targets conflict, by flexibly transferring authority from the driver to the assistance system as collision risk increases.

**Keywords** Human–machine cooperation · Steering control · Human–machine conflict · Nash game · Allocation of driving right

## List of Symbols

|                  |                                                                  |                                            |                                                                                           |
|------------------|------------------------------------------------------------------|--------------------------------------------|-------------------------------------------------------------------------------------------|
| $m$              | Total vehicle mass, kg                                           | $\delta_a, \delta_c$                       | Driver and driver assistance system output, rad                                           |
| $L$              | Wheelbase, M                                                     | $w$                                        | Driver control weight                                                                     |
| $l_f, l_r$       | Distances from the center of mass to the front and rear axles, m | $\theta_{sw}$                              | Steering wheel angle output, rad                                                          |
| $C_{lf}, C_{lr}$ | Longitudinal stiffness of the front and rear wheels, N/rad       | $T_1, T_2$                                 | Driver and driver assistance system reference trajectory                                  |
| $C_{cf}, C_{cr}$ | Front and rear wheel lateral stiffness, N/rad                    | $Q_1, Q_2$                                 | Driver and driver assistance system trajectory tracking precision weight matrix           |
| $S_f, S_r$       | Front and rear wheel slip ratio                                  | $R_1, R_2$                                 | Driver and driver assistance system control stability weight matrix                       |
| $\xi$            | System state variable                                            | $y_{a-y}, y_{c-y}$                         | Driver and driver assistance system reference lateral displacement, m                     |
| $A$              | System state variable coefficient matrix                         | $\varphi_{a-\varphi}, \varphi_{c-\varphi}$ | Driver and driver assistance system reference yaw angle, rad                              |
| $B_1, B_2$       | Driver and driver assistance system input coefficient matrix     | $q_{a-y}, q_{c-y}$                         | Driver and driver assistance system lateral displacement tracking precision weight factor |
| $C$              | System output coefficient matrix                                 | $q_{a-\varphi}, q_{c-\varphi}$             | Driver and driver assistance system reference yaw angle tracking precision weight factor  |
| $\eta$           | System output                                                    | $N_p$                                      | Prediction time domain in discrete model optimization                                     |

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