

# Development of Coordinator for Optimal Tireforces Distribution for Vehicle Dynamics Control Considering Nonlinear Tire Characteristics

Mooryong Choi<sup>1</sup> · Chulwoo Moon<sup>2</sup>

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## Abstract

The Vehicle Dynamics Control (VDC) system is designed to enhance vehicle stability by effectively applying corrective yaw moments through differential brake forces during severe maneuvers. The VDC configuration primarily comprises two essential components: the supervisor and coordinators. The supervisor is responsible for determining appropriate corrective yaw moments, while the coordinators decide the tire forces necessary to achieve the desired corrective yaw moments. In modern times, various control schemes, such as model predictive controls, h-infinity controls, and relative controls, have been extensively investigated for the supervisors. However, in contrast, research concerning the coordinator component has not received much attention, resulting in relatively low research numbers. Most of the research has focused on the utilization of VDC coordinators that decide tire forces solely in proportion to corrective yaw moments. This approach leads to significant errors due to assumptions that do not account for the nonlinear characteristics of tires. In this research analysis, a coordinator considering nonlinear tire characteristics, such as the friction ellipse effect is presented. This crucial method of considering tire's nonlinear characteristics significantly enhances the accuracy of achieving the corrective yaw moment. Overall, the developed coordinator was validated through both simulations and experiments.

**Keywords** Vehicle Dynamics Control · Optimal tire force distribution · Friction ellipse effect · Tire force nonlinearity

## List of Symbols

|            |                                           |
|------------|-------------------------------------------|
| $\delta_f$ | Average front steer angle                 |
| $C_f$      | Lumped cornering stiffness of front tires |
| $C_r$      | Lumped cornering stiffness of rear tires  |
| $\mu$      | Tire-road friction coefficient            |
| $F_x$      | Tire longitudinal force                   |
| $F_{yf}$   | Front axle lateral tire force             |
| $F_{yr}$   | Rear axle lateral tire force              |
| $l_f$      | CG-front axle distance                    |
| $l_r$      | CG-rear axle distance                     |
| $I_z$      | Vehicle yaw moment of inertia             |
| $m$        | Vehicle mass                              |

|          |                                               |
|----------|-----------------------------------------------|
| $v_x$    | Vehicle longitudinal speed                    |
| $M_z$    | Corrective yaw moment                         |
| $\tau_b$ | Time constant for lag of differential braking |
| $h$      | Height of mass center of gravity              |

## 1 Introduction

Vehicle safety demands have consistently grown since the advent of automotive vehicles. In the early stages, safety systems primarily comprised passive measures effective post-crash. Studies investigating airbags, seat belts, and dynamic human body models, coupled with numerous crash tests, were conducted to assess vehicle safety. As electronic technologies advanced and became more reliable, active safety systems, aimed at crash prevention, began entering the automotive market. After Following Robert Bosch GmbH's introduction of the first Antilock Braking Systems (ABS) in 1978, various active safety systems have entered

✉ Chulwoo Moon  
cwmoon@katech.re.kr

<sup>1</sup> Vehicle Control R&D Center, Nmotion, Incheon 22004, Korea

<sup>2</sup> Platform Safety Technology R&D Department, Korea Automotive Technology Institute, Chungnam 31214, Korea